



1.0 INPUT

1.1 Dimensions

Width of Corbel	b	=	200 mm
Horizontal Length	a	=	500 mm
Distance from Load to Column Face	a_v	=	400 mm
Free End Depth	h_1	=	250 mm
Overall Depth of Corbel	h	=	500 mm

1.2 Bearing Plate

Length of Bearing Plate	L_b	=	150 mm
Width of Bearing Plate	W_b	=	150 mm

1.3 Reinforcement

1.3.1 Main

No. of Bars	N_m	=	3
Diameter of Bar	D_m	=	20 mm

1.3.2 Shear

Diameter of Bar	D_s	=	10 mm
Spacing Between Stirrups	L_s	=	120 mm

1.3.3 Cover

Clear Cover	C_c	=	25 mm
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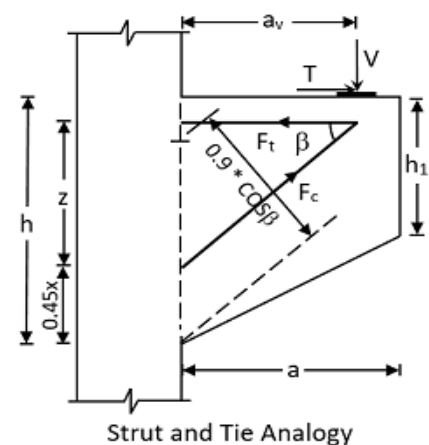
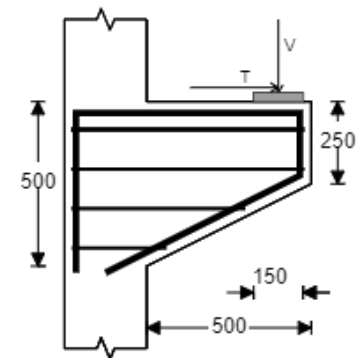
1.4 Loads

Ultimate Axial Load	V	=	250 kN
Ultimate Horizontal Load	T	=	30 kN
Service Axial Load	V_{sl}	=	150 kN
Service Horizontal Load	T_{sl}	=	20 kN

1.5 Materials

Concrete Grade	f_{cu}	=	25 N/mm ²
Main Reinforcement Grade	f_y	=	500 N/mm ²
Shear Reinforcement Grade	f_{yv}	=	460 N/mm ²
Modulus of Elasticity of Steel	E_s	=	200000 N/mm ²

1.6 Material Safety Factors



Concrete in Compression	γ_{mc}	= 1.5
Concrete in Shear	γ_{mcs}	= 1.25
Reinforcement	γ_{ms}	= 1.15

1.7 Crack Width

Check for Crack Width		Yes
Maximum Allowable Crack Width	W_k	= 0.35 mm

2.0 OUTPUT

Ref: BS 8110 - Part 1

2.1 Bearing Stress

Maximum Bearing Stress	f_b	= $0.8 * f_{cu} = \mathbf{20 N/mm^2}$	<i>Cl. 5.2.3.4</i>
Actual Bearing Stress	f_a	= $V / (W_b * L_b) = \mathbf{11.111 N/mm^2}$	

2.2 Reinforcement

Effective Depth	d	= $h - C_c - (D_m / 2) = \mathbf{465 mm}$
Horizontal Force	H	= $\max(T, 0.5 * V) = \mathbf{125 kN}$
Tension Reinforcement	A_{stp}	= 942.5 mm²

2.3 Strut and Tie Method

Lever arm Distance	z	= $d - 0.45 * x$	
Angle of Inclination	β	= $\cot^{-1}(a_v / z)$	
Steel Tension Force	F_t	= $V * a_v / z + T$	
Concrete Strut Force in Compression	F_c	= $V / \sin(\beta)$	
Depth of Neutral Axis (Iteration)	x	= $F_c * \gamma_{mc} / (0.603 * f_{cu} * b * \cos(\beta))$ = 250.8 mm	
Lever Arm Distance	z	= 352.2 mm	
Tensile Force on Steel Member	F_t	= 314 kN	
Concrete Strut Force in Compression	F_c	= 378.32 kN	
Design Moment	M_a	= $(V * a_v) + (H * z) = \mathbf{144 kNm}$	
Area of Reinforcement Required	A_{sreq}	= $M_a / ((f_y / \gamma_{ms}) * z) = \mathbf{940.6 mm^2}$	
Minimum Area of Reinforcement	A_{smin}	= $0.004 * b * h = \mathbf{400 mm^2}$	<i>Table: 3.25</i>
Maximum Area of Reinforcement	A_{smax}	= $0.04 * b * h = \mathbf{4000 mm^2}$	

2.4 Shear Design

Shear Stress	v	= $V / (b * d) = \mathbf{2.688 N/mm^2}$	<i>Cl.3.4.5.2</i>
Design Concrete Shear Stress	v_c	= 0.635 N/mm²	<i>Table: 3.8</i>
Enhanced Shear Stress	v'_c	= $2 * (d / a_v) * v_c = \mathbf{1.476 N/mm^2}$	<i>Cl.3.4.5.8</i>
Maximum Shear Stress	v_{max}	= $\min(0.8 * v'_{cu}, 5) = \mathbf{4 N/mm^2}$	<i>Cl.3.4.5.2</i>
Shear Strength Required	v_s	= $\max(v - v'_c, 0.4) = \mathbf{1.212 N/mm^2}$	
Area of Shear Reinforcement Required /m	A_{svreq}	= $\max(v_s * b / (f_{yv} / \gamma_{ms}), 0.5 * A_{sreq})$ = 606.1 mm²	<i>Table: 3.7</i>

Distribution Depth $d_d = (2/3) * d = 310 \text{ mm}$

2.5 Ultimate Anchorage Bond Stress

Tensile Force in Steel at Start of Bend $F_{bt} = (F_t / N_m) * (A_{sreq} / A_{stp}) = 104.4 \text{ kN}$

Design Ultimate Anchorage Bond Stress $F_{bu} = \beta * \sqrt{f_{cu}} = 2.5 \text{ N/mm}^2$ *Cl. 3.12.8.4*

Anchorage Bond Length Required $L_r = F_{bt} / (\pi * D_m * F_{bu}) = 664.9 \text{ mm}$ *Cl. 3.12.8.3*

Internal Radius of Bend $R = 4 * D_m = 80 \text{ mm}$

Bond Stress Limit $F_{lim} = (2/3) * F_{bt} / (R * D_m) = 43.52 \text{ N/mm}^2$

Bond Stress $F_{be} = (2 * f_{cu}) / (1 + (2 * D_m / (C_c + D_m))) = 26.471 \text{ N/mm}^2$

2.6 Crack Width Calculation

Ref: BS 8110 - Part 2

Spacing of Tension Bars $s = 333.3 \text{ mm}$

Modulus of Elasticity of Concrete $E_c = (20000 + 200 * f_{cu}) / 2 = 12500 \text{ N/mm}^2$

Modular Ratio $m = E_s / E_c = 16$

Depth of Neutral Axis (Iteration) $x = ((m * A_{stp}) / b) * (((1 + 2 * b * d) / (A_{stp} * m))^{1/2} - 1) = 199.9 \text{ mm}$

Lever Arm Distance $z = d - (x / 3) = 398.4 \text{ mm}$

Service Design Moment $M_s = (V_{sl} * a_v) + (T_{sl} * z) = 68 \text{ kNm}$

Stress in Reinforcement $F_s = M_s / (A_{stp} * z) = 178.567 \text{ N/mm}^2$

$\epsilon_1 = ((h - x) / (d - x)) * (F_s / E_s) = 0.001011$

$\epsilon_2 = (b * (h - x)^2) / (3 * E_s * A_{stp} * (d - x)) = 0.00012$

Average Strain $\epsilon = \epsilon_1 - \epsilon_2 = 0.000891$ *Eq. 13*

Distance of Crack to Nearest Tension Bar $a_{cr} = [(s / 2)^2 + (C_c + D_m / 2)^2]^{1/2} - (D_m / 2) = 160.298 \text{ mm}$

Design Surface Crack Width $W_{cr} = (3 * a_{cr} * \epsilon) / (1 + 2 * (a_{cr} - C_c) / (h - x)) = 0.225 \text{ mm}$ *Eq. 12*

3.0 SUMMARY

Description	Required	Actual	Status
Bearing Stress (N/mm ²)	$f_b \leq 20$	$f_a = 11.111$	PASS
Minimum Area of Reinforcement (mm ²)	$A_{smin} \geq 400$	$A_{stp} = 942.5$	PASS
Maximum Area of Reinforcement (mm ²)	$A_{smax} \leq 4000$	$A_{stp} = 942.5$	PASS
Area of Main Reinforcement (mm ²)	$A_{sreq} \geq 940.6$	$A_{stp} = 942.5$	PASS
Area of Shear Reinforcement (mm ² /m)	$A_{svreq} \geq 606.1$	$A_{svp} = 654.5$	PASS
Bond Stress (N/mm ²)	$F_{lim} \leq 43.52$	$F_{be} = 26.471$	PASS
Crack Width (mm)	$W_k \leq 0.35$	$W_{cr} = 0.225$	PASS